

Let us discuss the complexity of linear search and binary search.

### Linear Search Algo! →

1. Set Found equal to false.
2. Set  $loc$  equal to 1.
3. while  $loc \leq n$  and not found, do the following.
  4. if  $Item = A[loc]$  then.
    5. set found to True.
    6. else set increment  $loc$  by 1.

The worst case is obvious that is which item is not in the list.

So in the worst case we need to find the computing time for linear search algorithm as follows

Statement	# of times executed
1	1
2	1
3	1
4	$n+1$
5	$n$
6	0
	$n$
TOTAL	$3 + 3n$

$$T_L(n) = \underline{\underline{O(n)}}$$

## Binary Search Algo: →

1. Set found = false.

2. Set first = 1

3. Set last = n.

4. While first ≤ last and

not found do the following.

5. Calculate mid = (first + last) / 2

6. If Item < A[mid] then

set

7. last = mid - 1

8. Else if Item > A[mid] then

9. Set first = mid + 1

10. else set

found to True.

→ In this algorithm, statements 1, 2, and 3 are executed exactly once.

→ To calculate the worst case complexity, we must determine the number of passes (times) the loop composed of statements 4 through 10 is executed.

→ Each pass through the loop reduces the size of the sublist still to be searched by at least one half.

$$2 \quad 10/4 = 2$$

→ The last pass occurs when the sub list reaches size one.

→ Thus the total number of iterations of this loop is 1 plus the no. of  $k$  passes required to produce a sub list of size one.

→ Since the size of the sub list after  $k$  passes is at most  $n/2^k$ , we must have

$$\frac{n}{2^k} < 2$$

that is

$$n=25,$$

$$\textcircled{1} \frac{25}{2^1} = 12$$

$$\frac{25}{2^2} = \frac{25}{4} = 6$$

$$\frac{25}{2^3} = \frac{25}{8} = 3$$

$$\frac{25}{2^4} = \frac{25}{16} = 1 <$$