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Lecture for M.Sc. Physics II Semester students

Paper – III Quantum Mechanics – II

Unit- III: Identical Particle

SPIN FUNCTIONS for 3 Electron SYSTEM:-

The 3 spin electron system can be considered as a 1+2 e⁻ combination. It means we can combine electron (S=1/2) with the triplet two electron function (S=1) & with the singlet function (S=0). In the first case, we get two groups of three electron spin function that corresponds to S=1 & S=3/2. In the second case, we get a single group that corresponds to S=1/2. Thus, we get one quartet group of spin state S=3/2 & two distinct triplet groups of spin state S=1/2 or a total of 4+2+2=8 state individual of three electron spin state. This must be expressed as linear combination of the 2³=8 products of one electron spin functions. We thus obtain

	$(S_1 + S_2 + S_3)^2$	$S_{1z} + S_{2z} + S_{3z}$
(+ + +)	$15/4 \hbar^2$	$3/2 \hbar$
$3^{-1/2} [(+++) + (+-+) + (-++)]$	$5/4 \hbar^2$	$1/2 \hbar$
$3^{-1/2} [(-+-) + (--+) + (+--)]$	$5/4 \hbar^2$	$-1/2 \hbar$
(- - -)	$15/4 \hbar^2$	$-3/2 \hbar$

$$6^{-1/2} [2(-++) - (++) - (+-+)] \quad 3/4 \hbar^2 \quad \pm 1/2 \hbar$$

$$6^{-1/2} [(-+ -) + (- - +) - 2(+ -)] \quad 3/4 \hbar^2 \quad -1/2 \hbar$$

$$2^{-1/2} [(++ -) - (+ - +)] \quad 3/4 \hbar^2 \quad \pm 1/2 \hbar$$

$$2^{-1/2} [(-+ -) - (- - +)] \quad 3/4 \hbar^2 \quad -1/2 \hbar$$

The first four quadrature states are symmetric in the interchange of any pair of particles. The division of the four triplet states into two pairs is such that the first is symmetric in the interchange of particles 2 & 3, and second pair is anti-symmetric 2 & 3. The symmetry with respect to the interchange of other two pairs is characterized the 2×2 matrix. The matrix operate on either pair of triplet spin state that have the same value.