

M.Sc. II Sem

PHY-201 [Atomic and Molecular Physics]

Unit- III
Nuclear Magnetic Spectroscopy



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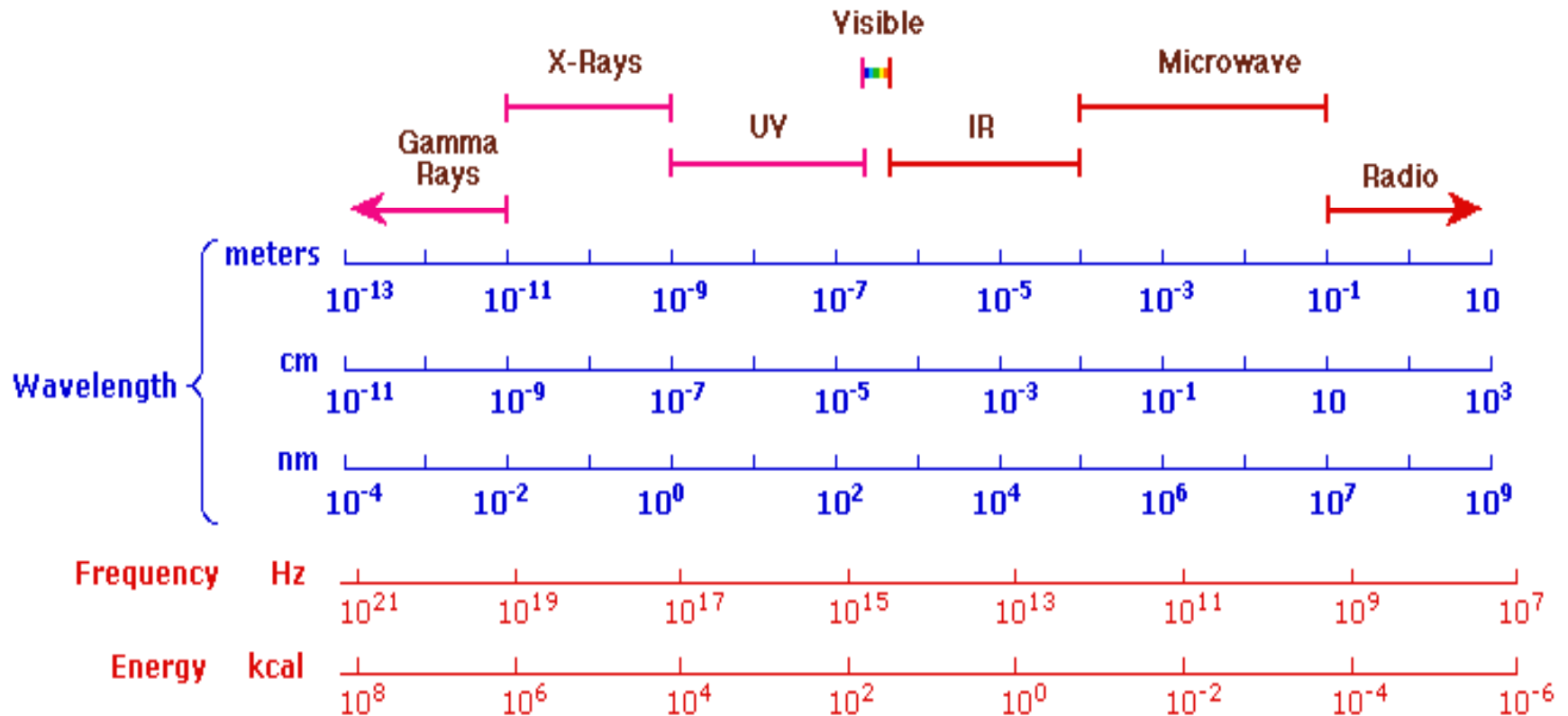
Outline

- ❖ Introduction to Spectroscopy
- ❖ Properties of Spin
- ❖ The Nuclear Magnetic Moment
- ❖ The Nuclear Spin Quantum Number
- ❖ Magnetic Properties of atomic Nuclei
- ❖ Nuclear precession in Magnetic field
 - Semi-Classical Description
 - Quantum mechanical Description
 - Quantum- classical correspondence

Introduction to Spectroscopy

Spectroscopy is the study of the interaction of electromagnetic radiation (light) with matter.

The Electromagnetic Spectrum





NMR uses electromagnetic radiation in the radio frequency range

- •Long wavelength, very low energy
- •Low energy has significant consequences:
- •Sharp signals (Good)
- •Poor sensitivity (Bad)
- •Longer experiment time (Bad)

Properties of Spin

Spin is a fundamental property of nature

- Any unpaired electron, proton, or neutron will possess a spin of $\frac{1}{2}$
- Atomic nuclei, which are composed of protons and neutrons, may also possess spin

The spin of an atomic nucleus is determined by the number of protons and neutrons

- Atoms with odd number of protons will have spin
- Atoms with odd number of neutrons will have spin
- Atoms with EVEN number of protons and neutrons will not have spin

The value of the nuclear spin is defined by **I** , the *nuclear spin quantum number* and can have values of ($I = 0, 1/2, 1, 3/2, 2, 5/2, \dots$)

A nucleus of spin **I** can exist in **$(2I+1)$** spin states.

The Nuclear Magnetic Moment

- All atomic nuclei can be characterized by a nuclear spin quantum number, I . I can be ≥ 0 and any multiple of $\frac{1}{2}$

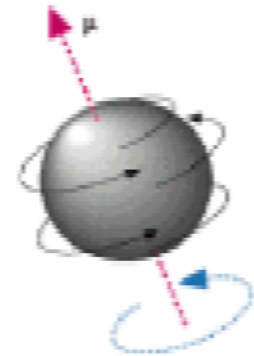
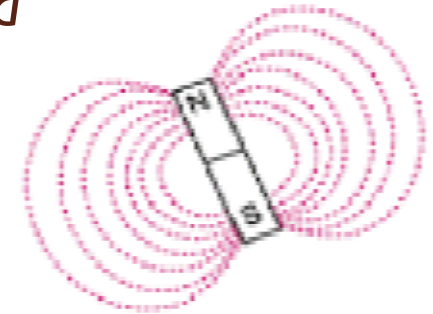
- Nuclei with $I = 0$ do not possess nuclear spin and consequently are termed 'NMR silent'.

- All nuclei with $I \neq 0$ possess spin, charge and angular momentum P , resulting in a nuclear magnetic moment μ .

$$\mu = \gamma P$$

Where γ is the gyromagnetic ratio of the nucleus.

Values of γ can be positive or negative and determine the sense of precession and thus the direction of the magnetic moment.



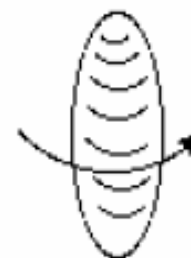
$I =$ the nuclear spin quantum number



No spin
 $I = 0$



Spinning sphere
 $I = 1/2$



Spinning ellipsoid
 $I = 1, 3/2, 2, \dots$

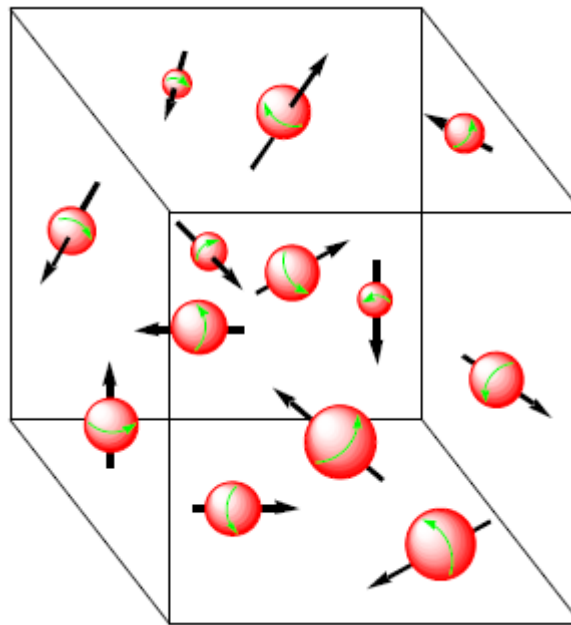
| For Nuclei of: | $I =$ | Example |
|-----------------------|--------------|--------------------------------|
| Odd Mass | Half Integer | $^1\text{H}, ^{13}\text{C}$ |
| Even Mass/Even Charge | Zero | $^{12}\text{C}, ^{16}\text{O}$ |
| Even Mass/Odd Charge | Integer | $^2\text{H}, ^{14}\text{N}$ |

If $I = 0$, NMR Inactive

If $I \geq 1$, Quadrupolar (non-spherical nuclear charge distribution)

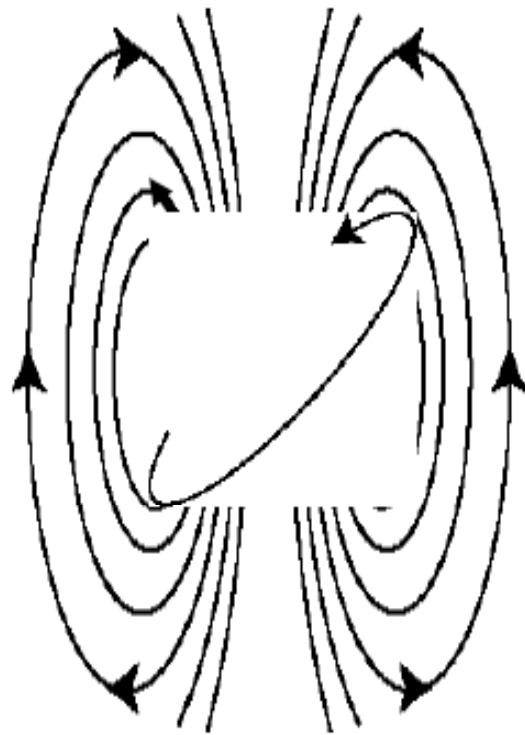
Magnetic properties of atomic nuclei

- The magnetic moment (μ) is a **vector quantity that has both magnitude and direction**
- In the absence of an external magnetic field the magnetic moments (μ) are **randomly orientated**.

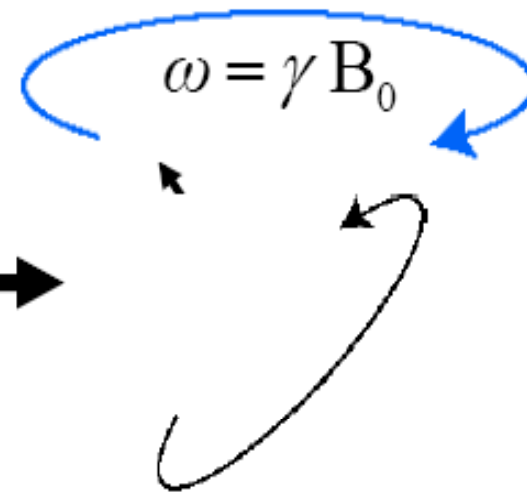


Nuclear Precession in a Magnetic Field

Semi-Classical Description



Magnetic Field B_0



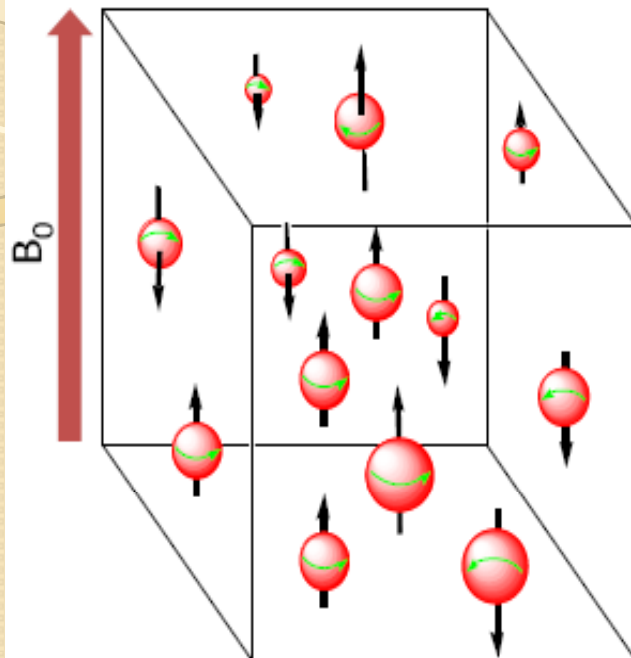
Example:

For ^1H nuclei (protons)
($\gamma = 2.68 \times 10^8 \text{ rad T}^{-1} \text{ s}^{-1}$)
in a magnetic field of
11.74 Tesla
 $\omega = 3.15 \times 10^9 \text{ rad s}^{-1}$
or
 $\nu = \omega / 2\pi = 5 \times 10^8 \text{ s}^{-1}$
= 500 MHz

The Magnetic Field (B_0) exerts torque on angular momentum (\mathbf{L}) and causes **Nuclear Precession**, analogous to precession of spinning top. The frequency of the precession (ω), often called the Larmor frequency, is proportional to the gyromagnetic ratio (γ) and the strength of the external magnetic field (B_0).

Nuclear Precession in a Magnetic Field

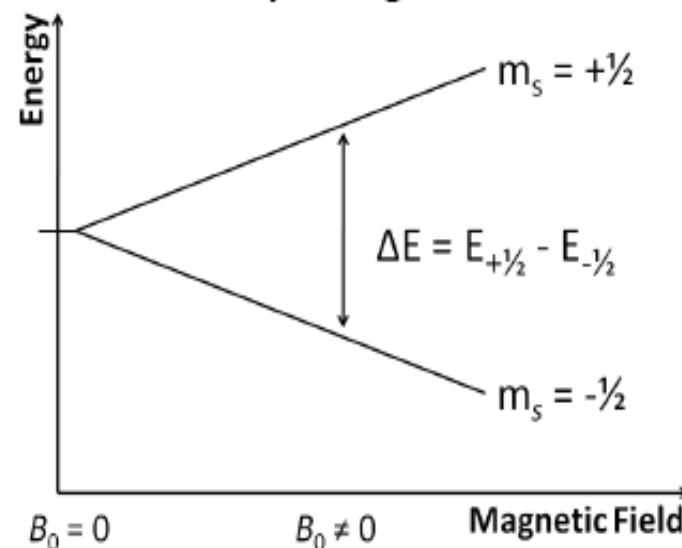
Quantum Mechanical Description



In the macroscopic world the two magnets can be aligned in an infinite number of orientations. At the atomic level, these alignments are **quantized** and the number of orientations (spin states) are equal to $2\mathbf{I}+1$. We will only deal with spin $\frac{1}{2}$ nuclei.

The different **quantized** orientations will each have an energy level determined by the Zeeman splitting

Zeeman Splitting

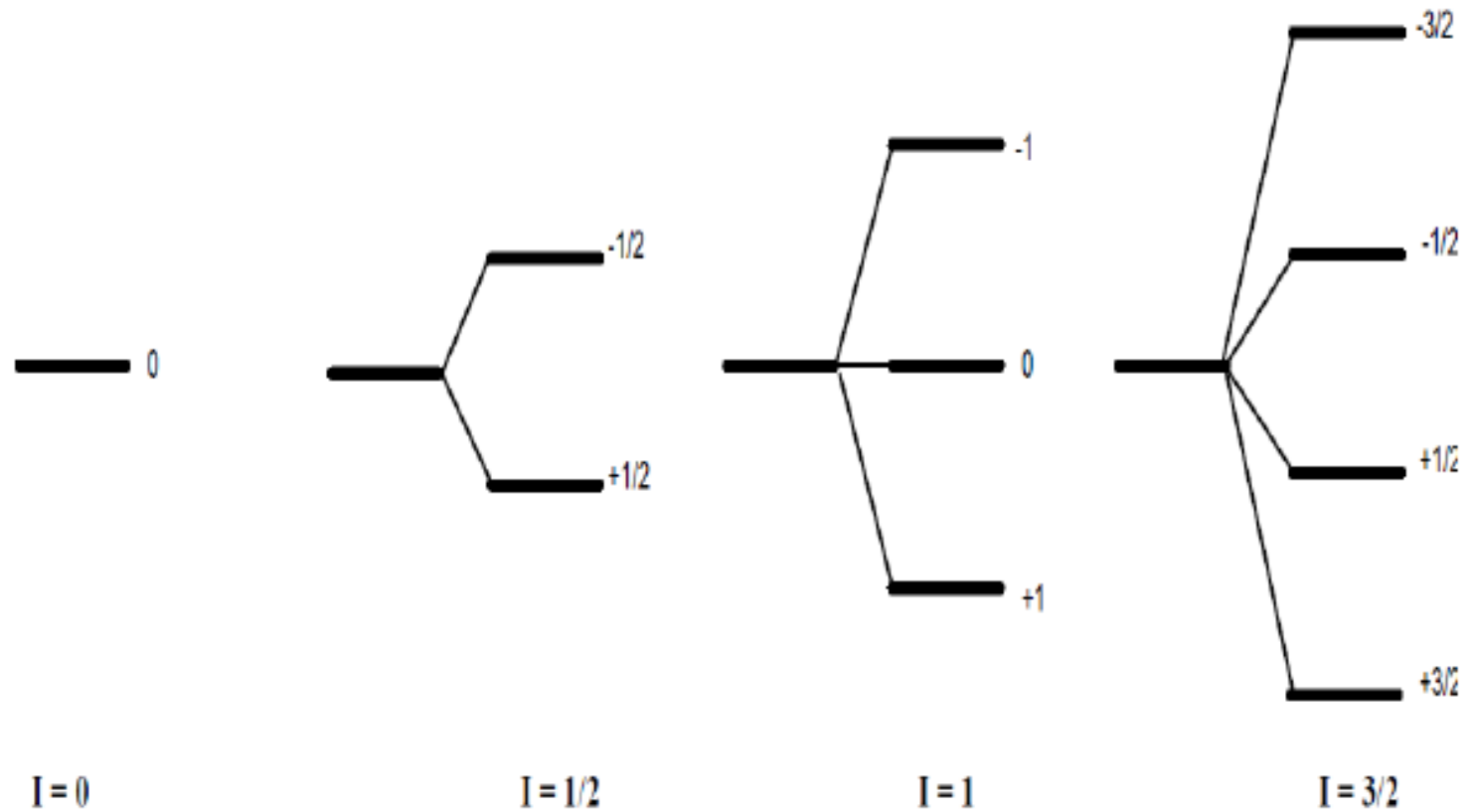


Nuclear Precession in a Magnetic Field

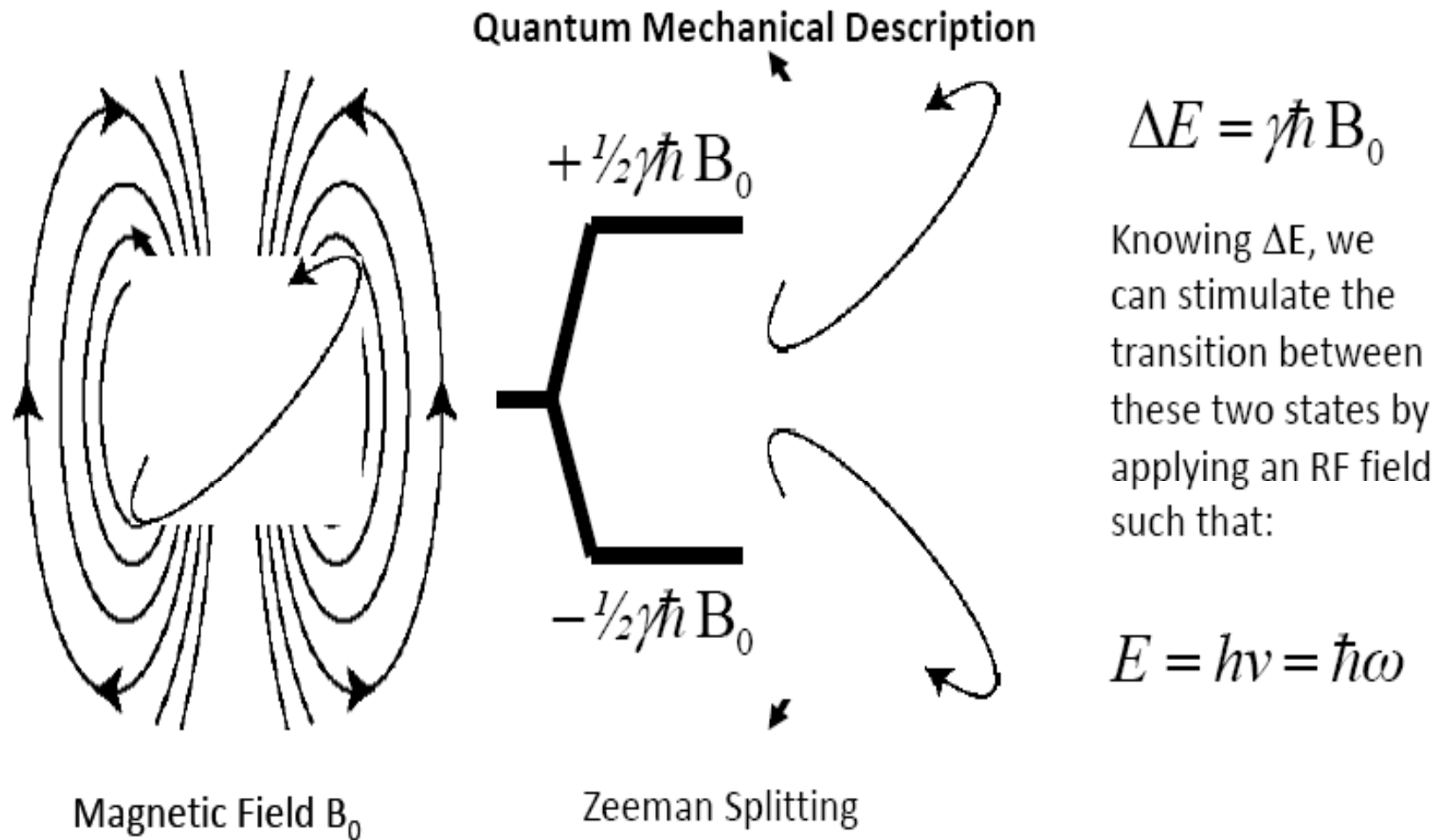
Quantum Mechanical Description

The energy levels are more complicated for $I > 1/2$

Zeeman Splitting



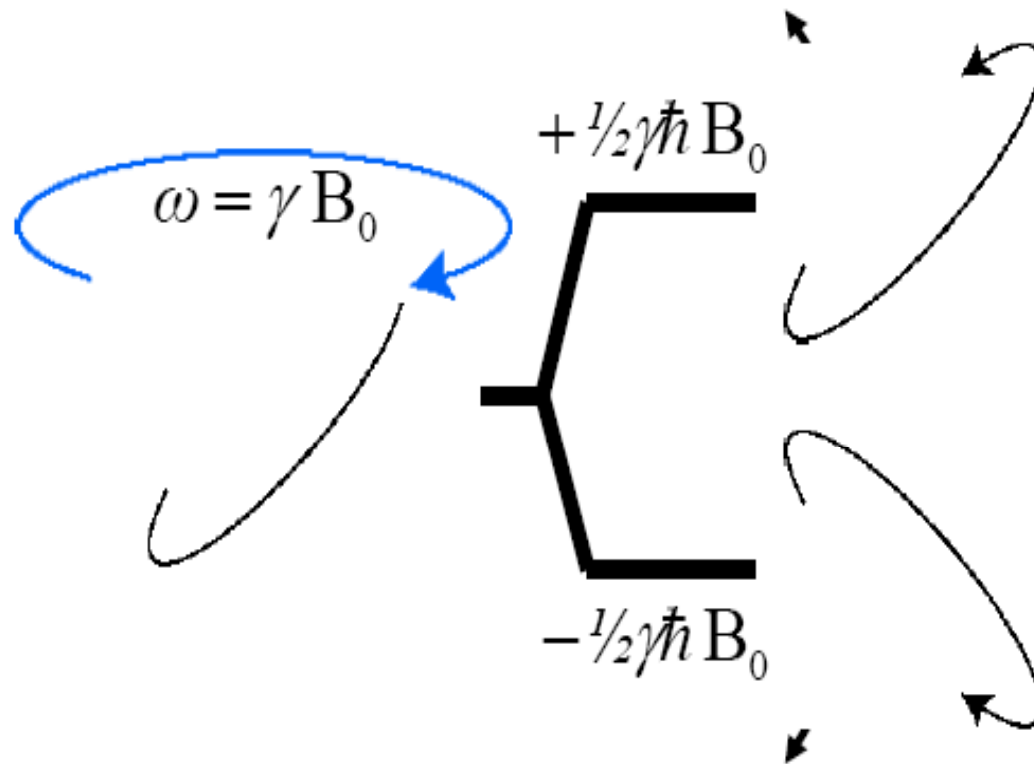
Nuclear Precession in a Magnetic Field



In NMR spectroscopy we are going to perturb the spin states by stimulating transitions between the energy levels.

Nuclear Precession in a Magnetic Field

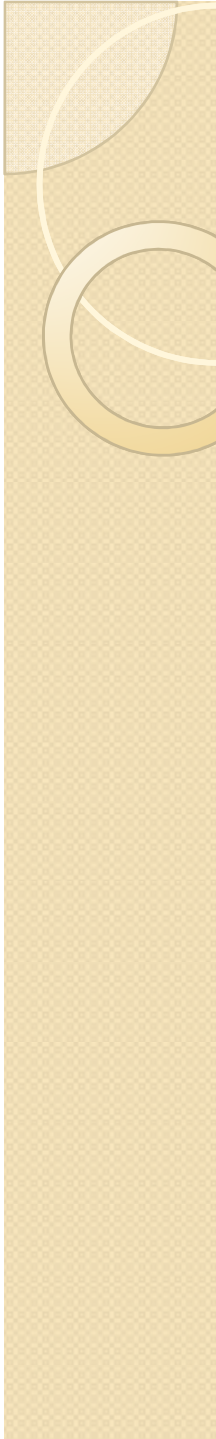
Quantum-Classical Correspondence



$$\Delta E = \gamma \hbar B_0$$

Knowing ΔE , we can stimulate the transition between these two states by applying an RF field which satisfies the resonance condition:

$$E = \hbar \omega = \gamma \hbar B_0$$



Thank You