

Analysis of frames subjected to Horizontal forces:-

The following approximate methods are in practice.

- (i) The Portal method.
- (ii) The Cantilever method.

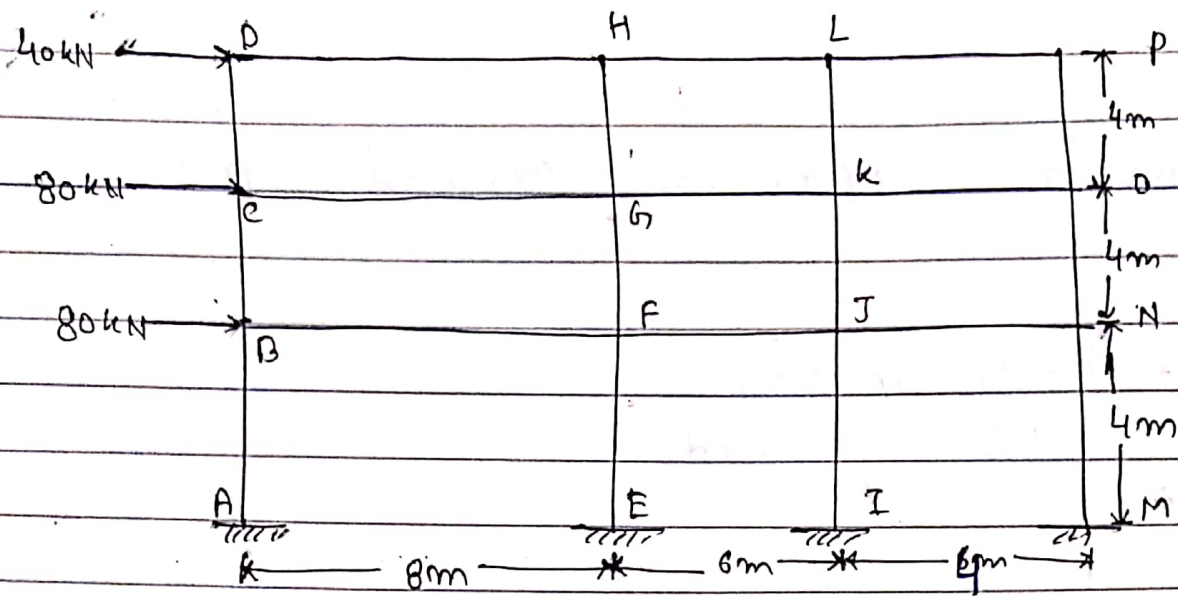
1. The Portal method:-

(a) Points of Contraflexure occur at the middle points of the members of the frame.

(b) Horizontal Shear taken by each exterior Column is double the Horizontal Shear taken by each of the internal Columns.

∴ By making the above two assumptions the structure can be easily analyzed.

Q. Analyse the frame:-



Solution

We will assume that points of contraflexure occur at the middle points of the individual members.

Column Shear

STOREY-3:-

$Q_3 =$ Shear for each end Column
 $\therefore 2Q_3 =$ Shear for each intermediate column

$$\therefore Q_3 + 2Q_3 + 2Q_3 + Q_3 = 40$$

$$Q_3 = \frac{20}{3} \text{ kN}$$

$$\therefore \text{Shear for end Column} = Q_3 = \frac{20 \text{ kN}}{3}$$

$$\therefore \text{Shear for intermediate Column} = 2Q_3 = 2 \times \frac{20}{3} = \frac{40}{3} \text{ kN}$$

STOREY-2

$$\therefore Q_2 = \text{Shear for each end Column}$$

$$\therefore 2Q_2 = \text{Shear for each intermediate Column}$$

$$Q_2 + 2Q_2 + 2Q_2 + Q_2 = 40 + 80$$

$$\boxed{Q_2 = 20 \text{ kN}}$$

$$\therefore \text{Shear for end Column} = Q_2 = 20 \text{ kN}$$

$$\therefore \text{Shear for intermediate Column} = 2Q_2 = 2 \times 20 \text{ kN} = 40 \text{ kN}$$

STOREY-3

$$\therefore Q_1 = \text{Shear for each end Column}$$

$$\therefore 2Q_1 = \text{Shear for intermediate Column}$$

$$Q_1 + 2Q_1 + 2Q_1 + Q_1 = 40 + 80 + 80$$

$$\boxed{Q_1 = \frac{100}{3} \text{ kN}}$$

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$$\therefore \text{Shear for end Column} = \frac{100}{3} \text{ kN}$$

$$\therefore \text{Shear for intermediate Column} = 201 \approx \frac{2 \times 100}{3} = \frac{200}{3} \text{ kN}$$

Column moment:-

Storey 3:-

$$\text{End Column. Moment at top or bottom} = \frac{20}{3} \times 2 = \frac{40}{3} \text{ kNm}$$

$$\begin{aligned} \text{intermediate Column. Moment at top or bottom} &= \frac{40}{3} \times 2 \\ &= \frac{80}{3} \text{ kNm} \end{aligned}$$

Storey 2:-

$$\text{End Column. Moment at top or bottom} = 20 \times 2 = 40 \text{ kNm}$$

$$\text{intermediate Column. Moment at top or bottom} = 40 \times 2 = 80 \text{ kNm}$$

Storey 1:-

$$\text{End Column. Moment at top or bottom} = \frac{100}{3} \times 2 = \frac{200}{3} \text{ kNm}$$

$$\text{intermediate Column. Moment at top or bottom} = \frac{200}{3} \times 2 = \frac{400}{3} \text{ kNm}$$

Beam moments :-

Storey 3 :-

$$M_{dh} = M_{dc} = \frac{40}{3} \text{ kN-m}$$

$$M_{hd} + M_{hc} = M_{he}$$

$$\frac{40}{3} + M_{hc} = \frac{80}{3}$$

∴

$$M_{hc} = \frac{40}{3} \text{ kN-m}$$

$$M_{ep} + M_{he} = M_{ek}$$

$$M_{ep} + \frac{40}{3} = \frac{40}{3} \times 2 = \frac{80}{3}$$

$$M_{ep} = \frac{40}{3} \text{ kN-m}$$

$$M_{ep} = M_{po} = \frac{40}{3} \text{ kN-m}$$

Storey - 2

$$M_{ch} = M_{cd} + M_{cb}$$

$$= \frac{40}{3} + 20 \times 40$$

$$= \frac{160}{3} \text{ kN-m}$$

$$M_{gc} = M_{ch} = \frac{160}{3} \text{ kN-m}$$

$$M_{ge} + M_{gk} = M_{gh} + M_{gf}$$

$$\frac{160}{3} + M_{gh} = \frac{80}{3} + 40 \times 2$$

$$M_{gk} = \frac{160}{3} \text{ kN-m}$$

Storey - 1

$$M_{bj} \theta = M_{be} + M_{ba}$$

$$M_{bj} = \frac{20 \times 2 + 200}{3}$$

$$M_{bj} = \frac{320}{3} \text{ kN-m}$$

$$M_{jb} + M_{bj} = M_{gf} + M_{fe}$$

$$\frac{320}{3} + M_{bj} = 80 + \frac{400}{3}$$

$$M_{bj} = \frac{320}{3} \text{ kN-m}$$

Shear in Beams:

$$S.F \text{ in DH} = \frac{2M}{L}$$

$$M = S.F \times \frac{L}{2}$$

$$S.F = \frac{2M}{L}$$

$$S.F \text{ in DH} = \frac{2 \times \frac{40}{3}}{8} = \frac{10}{3}$$

$$S.F \text{ in JN} = \frac{2 \times \frac{320}{3}}{4} = \frac{160}{3}$$

$$S.F \text{ in HI} = \frac{2 \times \frac{40}{3}}{6} = \frac{40}{9} \text{ kN}$$

$$S.F \text{ in LP} = \frac{2 \times \frac{40}{3}}{4} = \frac{20}{3}$$

$$S.F \text{ in CG} = \frac{2 \times \frac{160}{3}}{8} = \frac{40}{3} \text{ kN}$$

$$S.F \text{ in GK} = \frac{2 \times \frac{160}{3}}{6} = \frac{160}{9}$$

$$S.F \text{ in KO} = \frac{2 \times \frac{160}{3}}{4} = \frac{80}{3} \text{ kN}$$

$$S.F \text{ in BF} = \frac{2 \times \frac{320}{3}}{8} = \frac{80}{3} \text{ kN}$$

$$S.F \text{ in FJ} = \frac{2 \times \frac{320}{3}}{6} = \frac{320}{9} \text{ kN}$$