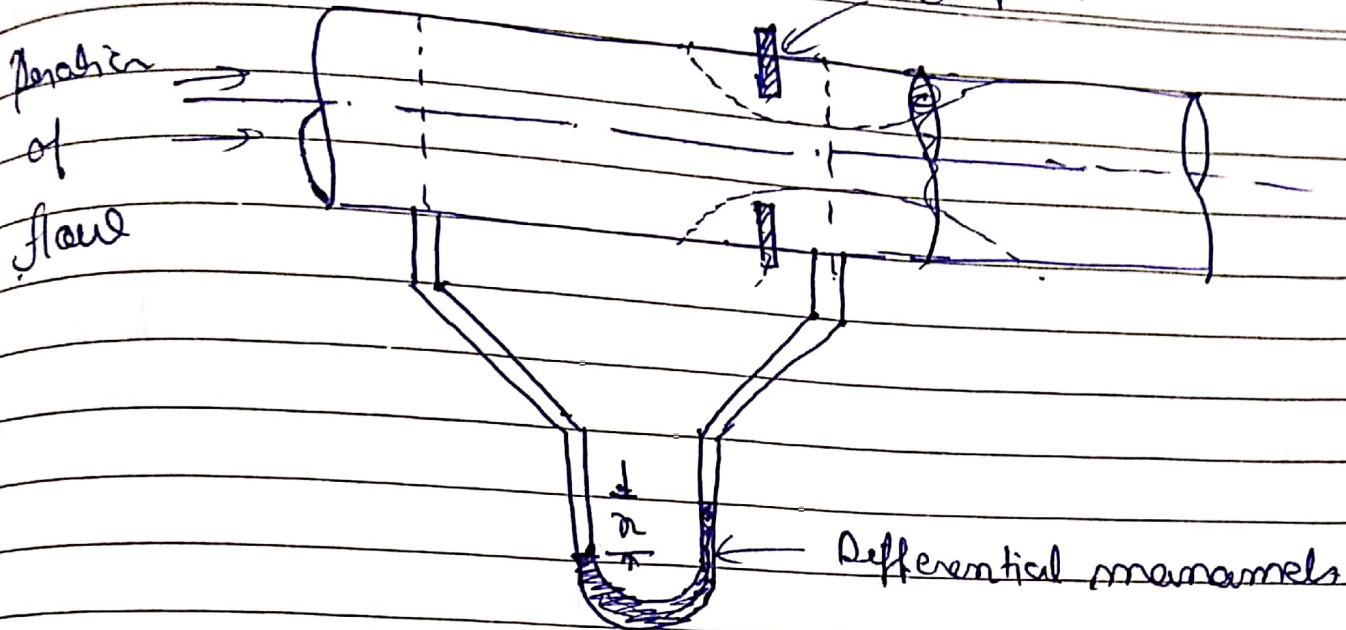


ORIFICE METER

It is a device used for measuring the rate of flow of a fluid through a pipe.

- It is a cheap device as compared to Venturi meter.
- It works on the same principle as that of Venturimeter.
- It consists of a circular plate which has a circular sharp edge hole called orifice, which is concentric with the pipe.
- Orifice dia is kept generally 0.5 times the dia of the pipe. However, it may vary from 0.4 to 0.8 times the pipe dia.
- A differential manometer is connected at section (1) and section (2).



let. P_1 = Pressure at section 1-1
 V_1 = Velocity at section 1-1
 a_1 = area of pipe at section 1-1

P_2, V_2, a_2 are corresponding value at section (2)

Apply Bernoulli's equation at section 1-1 and 2-2

$$\frac{P_1}{\rho g} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{V_2^2}{2g} + z_2$$

$$\left(\frac{P_1}{\rho g} + z_1 \right) - \left(\frac{P_2}{\rho g} + z_2 \right) = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$$

$$\left(\frac{P_1}{\rho g} + z_1 \right) - \left(\frac{P_2}{\rho g} + z_2 \right) = h = \text{Differential head}$$

$$h = \frac{V_2^2}{2g} - \frac{V_1^2}{2g}$$

$$V_2 = \sqrt{2gh + V_1^2}$$

Now section (2) is at the vena contracta and a_2 represent the area at the area of vena contracta
if a_0 is the area of orifice

$$C_c = \frac{a_2}{a_0}$$

where $C_c =$ Coefficient of contraction

$$a_1 V_1 = C_c = \frac{a_2}{a_0}$$

$$a_2 = a_0 C_c$$

by continuity eqⁿ

$$a_1 V_1 = a_2 V_2$$

$$V_1 = \frac{a_2}{a_1} V_2 = \frac{a_0 C_c}{a_1} V_2$$

$$V_2 = \sqrt{2gh + \frac{a_0^2 C_c^2 V_2^2}{a_1^2}}$$

$$v_2^2 = 2gh + \left(\frac{a_0}{a_1}\right)^2 c_c^2 v_2^2$$

$$v_2^2 \left[1 - \left(\frac{a_0}{a_1}\right)^2 c_c^2 \right] = 2gh$$

$$v_2 = \frac{\sqrt{2gh}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 c_c^2}}$$

then discharge

$$Q = v_2 \times a_2$$

$$= v_2 \times a_0 c_c$$

$$= \frac{a_0 c_c \sqrt{2gh}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 c_c^2}}$$

$$c_d = \frac{c_c \sqrt{1 - \left(\frac{a_0}{a_1}\right)^2}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 c_c^2}}$$

$$c_c = c_d \frac{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 c_c^2}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2}}$$

$$Q = a_0 \times C_d \frac{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 C_c^2}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2}} \times \frac{\sqrt{2gh}}{\sqrt{1 - \left(\frac{a_0}{a_1}\right)^2 C_c^2}}$$

$$Q = \frac{C_d a_0 a_1 \sqrt{2gh}}{\sqrt{a_1^2 - a_0^2}}$$