

★ Compass Survey :->

⊕ System of angle measurement :->

① Most widely used system

34

1 circumference = 360° degree

1 degree = 60 min

1 minute = 60 sec

⊕ Hour System

1 circumference = 24 hours

1 hour = 60 min

1 min = 60 sec

Note -> 1 circumference is according to the earth rotation

⊕ Centesimal System

1 circumference = 400 grade

1 grade = 100 centigrade

1 centigrade = 100 centi-centigrade

Important terms :->

① Bearing :-> The direction of a line w.r. to a given meridian. It is the angle b/w given meridian and the line.

② True meridian :-> Line joining true North and true South pole the earth is called True meridian.

↳ True north or south point are the point about which earth is rotating.

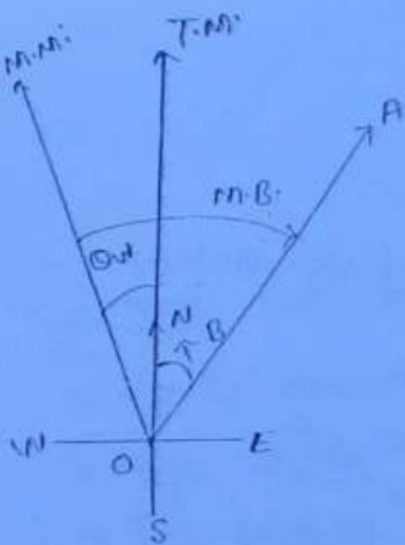
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③ True bearing: → Bearing measured from true meridian.

④ Magnetic Meridian: → Line joining magnetic North and South poles. - (35)

Magnetic bearing: → Bearing measured from magnetic meridian.

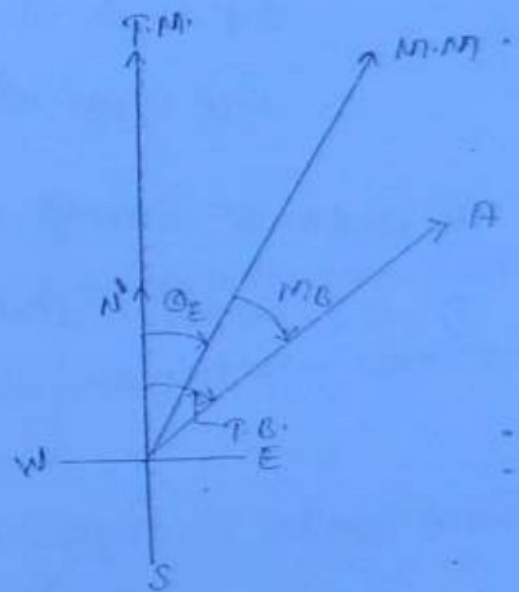
⑤ Magnetic declination: → Horizontal angle b/w true meridian and magnetic meridian at a particular place is called magnetic declination.



(Western Declination)

$$M.B. = T.B. + \theta_w$$

$$T.B. = M.B. - \theta_w$$



(Eastern declination)

$$M.B. = T.B. - \theta_e$$

$$T.B. = M.B. + \theta_e$$

⑦ Variation in Declination: →

Types: →

① Diurnal variation (Daily)

② Annual variation (Annually)

③ Secular variation (Due to the moment of moon)

④ Irregular variation.

★ ⑥ Angle of Dip: → IF a magnet is hanged freely from it's C.G. It aligns itself in the direction of magnetic flux in that area, angle made with horizontal direction of magnet is called dip angle.

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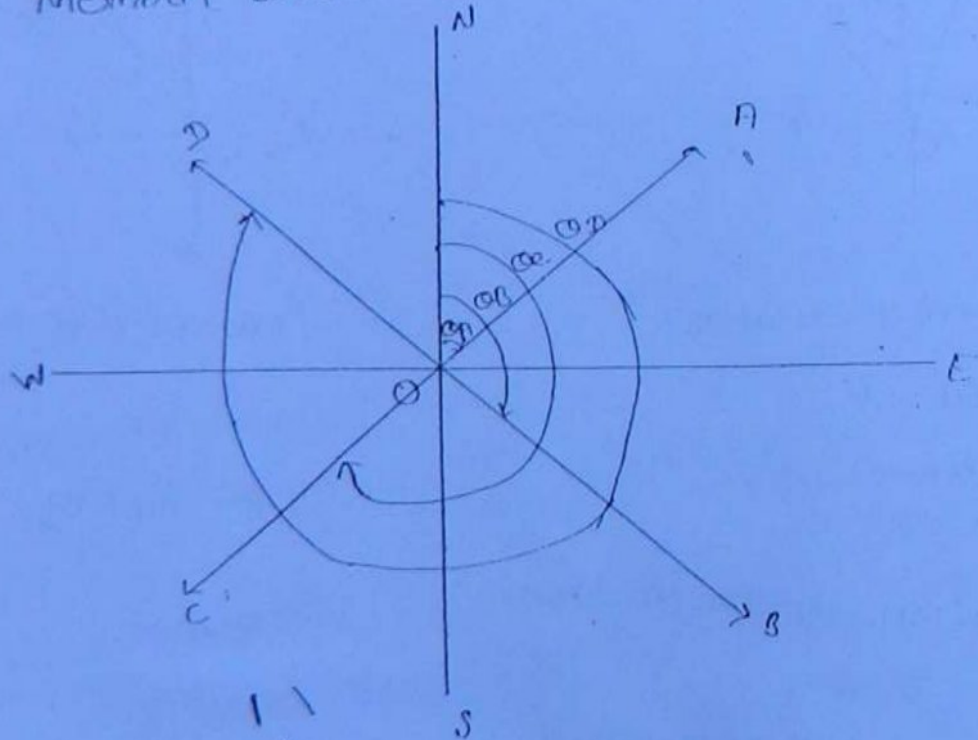
Dip angle at any point on earth is the angle b/w horizontal and direction of magnetic flux.

Dip angle at equator = 0

Dip angle at poles = 90°

⑦ System of Bearing measurement: →

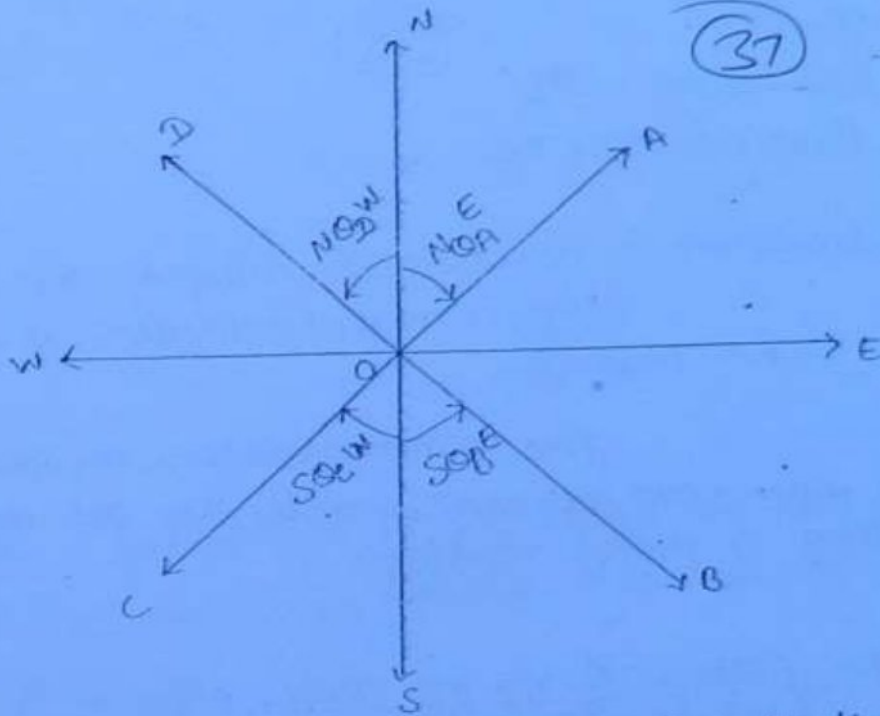
① WCB method (whole circle bearing method) →



→ All angle are measured from north.

→ always in clockwise direction.

② C.S.B. Method: \rightarrow
 (Quadrantal System of bearing)



- \rightarrow Angle are measured either from North or from South.
- \rightarrow Can be measured in clockwise / anticlockwise direction.
- \rightarrow Angle with direction are shown.
- \rightarrow This bearing system is also known as reduced bearing.

③ Fore bearing and Back bearing: \rightarrow



\rightarrow For line AB

Angle at 1st point A = $\angle OA$ = Fore bearing.

angle at 2nd point B = θ_B = Back bearing

→ for line BA

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Fore bearing = θ_B

Back bearing = θ_A

* Local Attraction: → Bearings of different line are measured using a magnetic needle. (in case of magnetic bearing)

Due to the presence of some iron objects near instrument, magnetic needle may get deflected, resulting in wrong readings.

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Problem: → The following readings were noted in a closed traverse

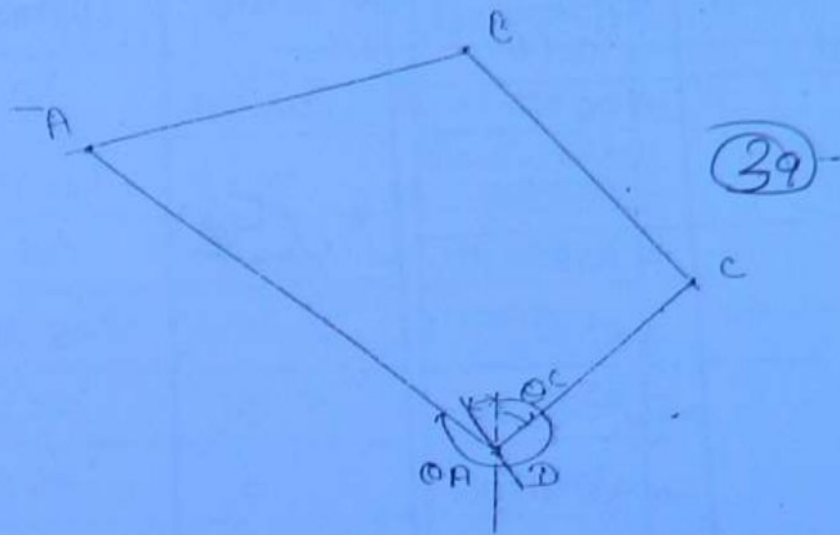
	Fore bearing	Back bearing
AB	32°	212° → 190°
BC	77°	262° → 185°
CD	112°	287° → 175°
DE	122°	302° → 180°
EA	265°	85° → 190°

This station is correct from local attraction

at what station do you suspect local attraction? Find correct bearing of the line. what will be the true bearings (as reduced bearing is magnetic declination was 12'W)

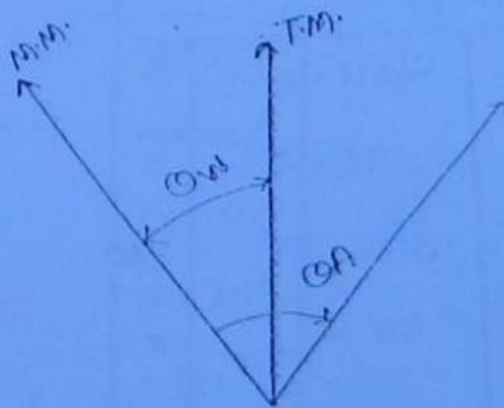
Solution: →

Line	Bearing	Correction	Corrected bearing
AB	32	✓ 0	32°
BA	212	✓ 0	212°
BC	77	✓ 0	77°
CB	262	✗ -5'	← 77 + 180 = 257
CD	112	✗ -5'	→ 112 - 5' = 107°
DC	287	✓ 0	↓ 107 + 180 = 287°
DE	122	✓ 0	122°
ED	302	✓ 0	↓ 122



→ Here all differences of FB/BB are 0, except for line BC and CD so station 'c' is affected from local attraction.

EA	265 ✓	0	265
AE	85 ✓	0	85



$$T.B = M.B - \theta_w$$

True bearing in $^{\circ}$ CB Method	True bearing in $^{\circ}$ CB
20	N 20 E
200	S 20 W
65	N 65 E
245	S 65 W
95	S 85 E
275	N 85 W
110	S 70 E
290	N 70 W
253	S 73 W
73	N 73 E

(90)

Problem \rightarrow following bearings were taken using a compass. Find out the correct bearing

AB	$75^{\circ} 5'$	$250^{\circ} 20'$	X
BC	$115^{\circ} 20'$	$296^{\circ} 35'$	X
CD	$165^{\circ} 35'$	$345^{\circ} 35'$	180°
DE	$224^{\circ} 50'$	$44^{\circ} 5'$	X
EA	304°	$125^{\circ} 5'$	X

Solution: when station C and D are free from local attraction

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Lines	Bearings	Correction	Corrected bearing
AB	75° 5'	+0° 30'	75° 35'
BA	250° 20'	+1° 15'	255° 35'
BC	115° 20'	+1° 15'	116° 35'
CB	296° 35'	0	296° 35'
CD	165° 35'	0	165° 35'
DC	305° 35'	0	305° 35'
DE	224° 50'	0	224° 50'
ED	44° 5'	+0° 45'	44° 50'
EA	304° 50'	+0° 45'	305° 35'
AE	135° 5'	+0° 30'	135° 35'

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Problem: → Following are the bearings of a closed traverse:

	FB	BB
AB	142° 30'	322° 30'
BC	223° 15'	40° 15'
CD	287°	107° 45'
DE	12° 25'	193° 15'
EA	60°	239°

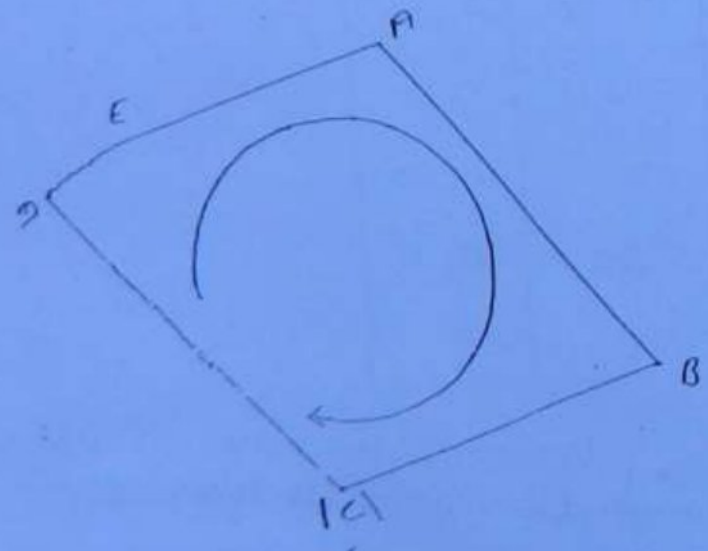
Considered AB value as correct and set the correct bearing of all other lines.

Solution: →

Lines	Bearing	Correction	Correct Bearing
AB	142° 30'	0	142° 30'
BA	322° 30'	0	322° 30'
BC	223° 15'	0	223° 15'
CB	44° 15'	-1° 0'	43° 15'
CD	287°	-1° 0'	286°
DC	107° 45'	-1° 45'	106°
DE	12° 45'	-1° 45'	11°
ED	193° 15'	-2° 15'	191° 15'
EA	60°	-2° 15'	57° 45'
AE	239°	not equal	237° 45'

(42)

Method of Internal angle:→
 1) Draw the traverse.



② Draw a clock wise circular direction.

③ Internal angles

(43)

$$A = \overset{\text{left}}{\angle E} - \overset{\text{right}}{\angle B} = 237 - 142' 30'' = 96' 30''$$

$$B = \angle A - \angle C = 322' 30'' - 223' 15'' = 99' 15''$$

$$C = \angle B - \angle D = 44' 15'' - 287' + 36'' = 117' 015''$$

$$D = \angle C - \angle E = 107' 45'' - 12' 45'' = 95'$$

$$E = \angle D - \angle A = 193' 15'' - 60'' = 133' 15''$$

$$\underline{\underline{541' 15''}}$$

④ IF any angle is 360° deduct 360°

⑤ IF any angle is negative add 360°

$$\begin{aligned} \text{Sum of all internal angles} &= (2n-4) \times 90^\circ \\ &= (2 \times 5 - 4) \times 90^\circ \\ &= 540^\circ \end{aligned}$$

$$\text{Difference in sum of internal angle} = 1' 15''$$

$$\text{Error in each angle} = \frac{1' 15''}{5} = 0' 15''$$

then correction in each angle = $(-)$ $0' 15''$
corrected internal angle.

$$96' 15''$$

$$99'$$

$$117'$$

$$194' 45''$$

$$133'$$

$$\underline{\underline{540''}}$$

$$A = AE - AB = 96^{\circ} 15' = \angle A$$

$$B = BA - BC = 99^{\circ} = \angle B$$

(14)

$$C = CB - CD + 360 = 117^{\circ}$$

$$D = DC - DE = 94^{\circ} 45'$$

$$E = ED - EA = 133^{\circ} = \angle E$$

Corrected bearing of line: \rightarrow

$$AB = 142^{\circ} 30'$$

$$+ \angle A = + 96^{\circ} 15'$$

$$AE = \frac{238^{\circ} 45'}{-180^{\circ}}$$

$$EA = 58^{\circ} 45'$$

$$+ \angle E = 133^{\circ}$$

$$ED = \frac{191^{\circ} 45'}{-180^{\circ}}$$

$$DE = 11^{\circ} 45'$$

$$+ \angle D = + 94^{\circ} 45'$$

$$DC = \frac{106^{\circ} 30'}{+180^{\circ}}$$

$$CD = 286^{\circ} 30'$$

$$+ \angle C = 117^{\circ}$$

$$- 360^{\circ}$$

$$CB = 43^{\circ} 30'$$

$$CB = 43^{\circ} 30'$$

$$- 180$$

$$BC = 223^{\circ} 30'$$

$$+ \angle B = 99^{\circ}$$

$$BA = 322^{\circ} 30'$$

$$- 180^{\circ}$$

$$AB = 142^{\circ} 30'$$

(11)

$$\begin{aligned}
 A = AB - AE &= 191^{\circ}30' - 53' = 138^{\circ}30' \\
 B = BC - BA &= 69^{\circ}30' - 13' = 56^{\circ}30' \\
 C = CD - CB &= 32^{\circ}15' - 246^{\circ}30' = 145^{\circ}45' \\
 &\quad + 360' \\
 D = DE - DC &= 262^{\circ}45' - 210^{\circ}30' = 52^{\circ}15' \\
 E = EA - ED &= 230^{\circ}15' - 80^{\circ}45' = 149^{\circ}30' \\
 &\quad \underline{542^{\circ}30'}
 \end{aligned}$$

$$\text{Total error} = 2^{\circ}30' \quad (46)$$

$$\begin{aligned}
 \text{Error in each angle} &= \frac{2^{\circ}30'}{5} \\
 &= 0^{\circ}30'
 \end{aligned}$$

$$\text{Correction in each angle} = (-) 0^{\circ}30'$$

Corrected angle

138°

56°

145°15'

52°15'

149°

AB has mini error

$$\text{Corrected bearing AB} = 191^{\circ}30' - 0^{\circ}45' = 190^{\circ}45'$$

$$\text{" " BA} = 13' + 0^{\circ}45' =$$

} this value is
range than

$$\text{corrected bearing AB} = 191^{\circ}30' + 0^{\circ}45' = 192^{\circ}15'$$

$$\text{" " BA} = 13' - 0^{\circ}45' = 12^{\circ}15'$$

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$$AB = 192' 15''$$

$$\angle A = -139'$$

$$AE = \begin{array}{r} 54' 15'' \\ + 180' \\ \hline \end{array}$$

$$EA = 234' 15''$$

$$\angle E = -149'$$

$$ED = \begin{array}{r} 85' 15'' \\ + 180' \\ \hline \end{array}$$

$$DE = 265' 15''$$

$$-\angle D = -151' 45''$$

$$DC = \begin{array}{r} 213' 30'' \\ - 180' \\ \hline \end{array}$$

$$CD = 33' 30''$$

$$\angle C = \begin{array}{r} -115' 15'' \\ + 360' \\ \hline \end{array}$$

Because the value is negative than add 360.

$$CB = \begin{array}{r} 248' 15'' \\ - 180' \\ \hline \end{array}$$

$$BC = 68' 15''$$

$$-\angle B = -56'$$

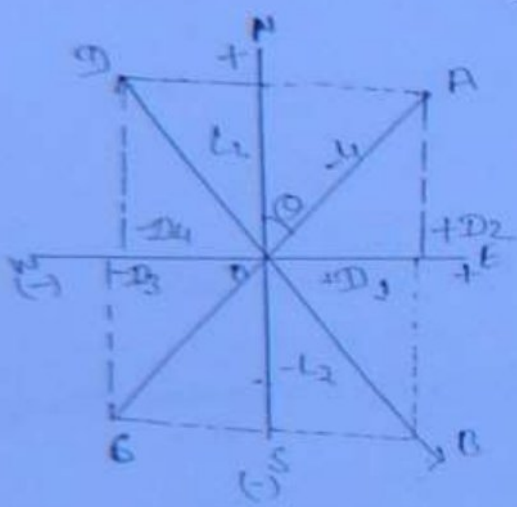
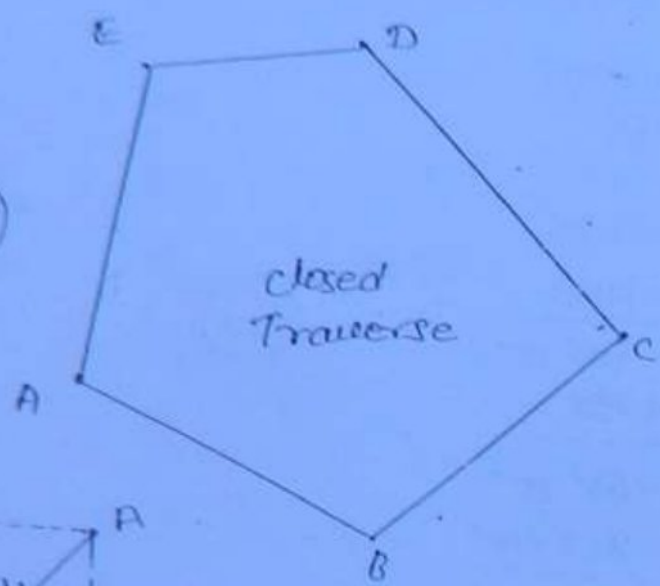
$$BA = \begin{array}{r} 12' 15'' \\ + 180' \\ \hline \end{array}$$

$$AB = 192' 15''$$

(47)

Traverse :→ latitude and departure of different sides of a traverse.

(48)



→ Latitude is the projection of a line on N-S direction

$$L = l \cos \theta$$

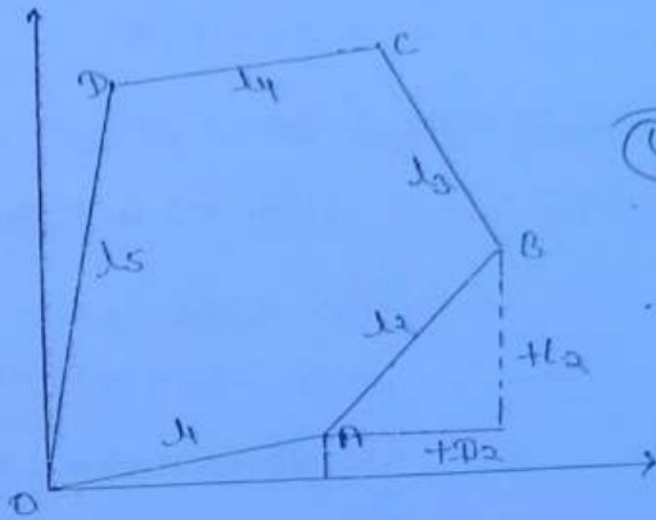
→ Departure is the projection of line on E-W direction

E-W direction

$$D = l \sin \theta$$

Side	WCB	Latitude	Departure
l_1	$0 < \theta < 90^\circ$	N θ_1 E $+l_1 \cos \theta_1$	$+l_1 \sin \theta_1$
l_2		S θ_2 E $-l_2 \cos \theta_2$	$+l_2 \sin \theta_2$
l_3		S θ_3 W $-l_3 \cos \theta_3$	$-l_3 \sin \theta_3$
l_4		N θ_4 W $+l_4 \cos \theta_4$	$-l_4 \sin \theta_4$

(11) Independent Co-ordinate :->



(49)

If co-ordinate of different points are measured w.r. to a fixed origin is called independent co-ordinate.

A) Properties of a closed traverse :->

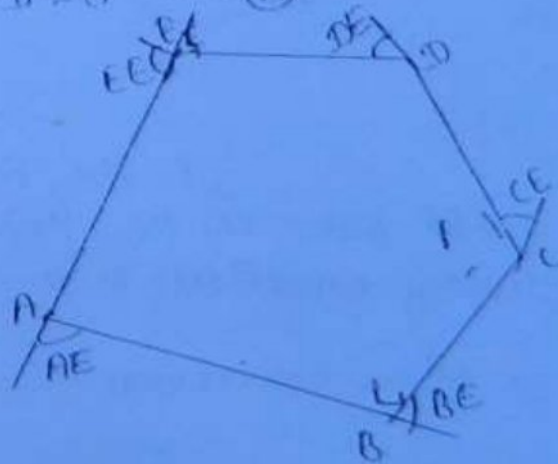
(1) Sum of all latitude and departure should be zero

$$l_1 \cos \theta_1 + l_2 \cos \theta_2 + \dots$$

$$EL = 0 \quad \text{--- (1)}$$

$$l_1 \sin \theta_1 + l_2 \sin \theta_2 + \dots$$

$$ED = 0 \quad \text{--- (2)}$$



② Sum of all internal angle of a closed traverse
 $= (2n-4) 90^\circ$

③ Sum of External angle of a closed traverse
 $AE + BE + \dots = (180 - A) + (180 - B) + \dots$

$= n \times 180 - (A + B + \dots)$

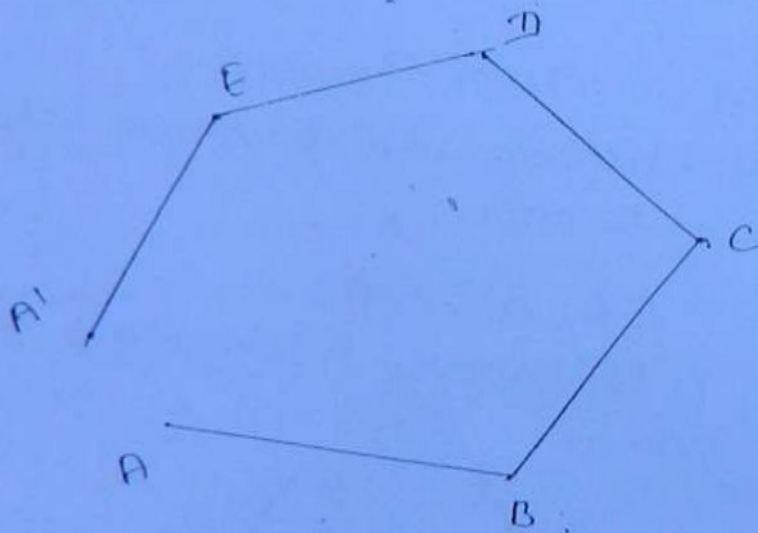
$= 2n \times 90 - (2n-4) \times 90$

$= 2n \times 90 - 2n \times 90 + 4 \times 90$

$= 360^\circ$

(50)

to close error: \rightarrow In case of a closed traverse



IF the first point of the closed traverse is not same as the that point. the error is called closing error. AA' is the error

$\therefore AA' = \text{Correction}$

* Adjustment of closing error: →

- ① $\sum L = 0$
- $\sum D = 0$

② Sum of all internal angle = $(2n-4) \times 90^\circ$

Method for balancing a closed traverse.

① Bowditch method.

② Transit method.

③ Graphical method

④ Pict method.

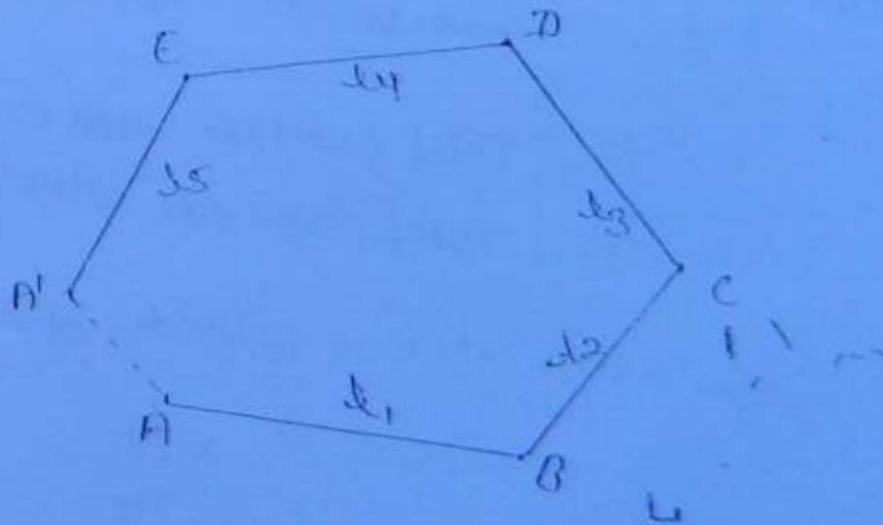
(5)

① Bowditch method: → This method is suitable when linear and angular measurements having been measured with equal precision. Changes of error are same in linear/ angular measurements.

As per Bowditch

① Error in linear measurement $\propto \sqrt{L}$

② Error in angular measurement $\propto \sqrt{L}$



IF

ΣL = Total error in latitude.
(Sum of all latitude with sign)

ΣD = Total error in Departure
(Sum of all departure with sign)

ΣL = Sum of all length of different line

Correction in latitude of a particular line

$$\textcircled{52} \quad C_L = \Sigma L \times \frac{l_i}{\Sigma L} \quad \text{--- (1)}$$

Correction in Departure

$$C_D = \Sigma D \times \frac{l_i}{\Sigma L} \quad \text{--- (2)}$$

⑤ Transit method \rightarrow This method is suitable when angular measurement are more precise than linear measurement.

Error $\left\{ \begin{array}{l} \Sigma L = \text{Sum of all latitudes (with sign)} \\ \Sigma D = \text{Sum of all departure (with sign)} \end{array} \right.$

L_T = Total latitude with out sign

D_T = Total Departure with out sign

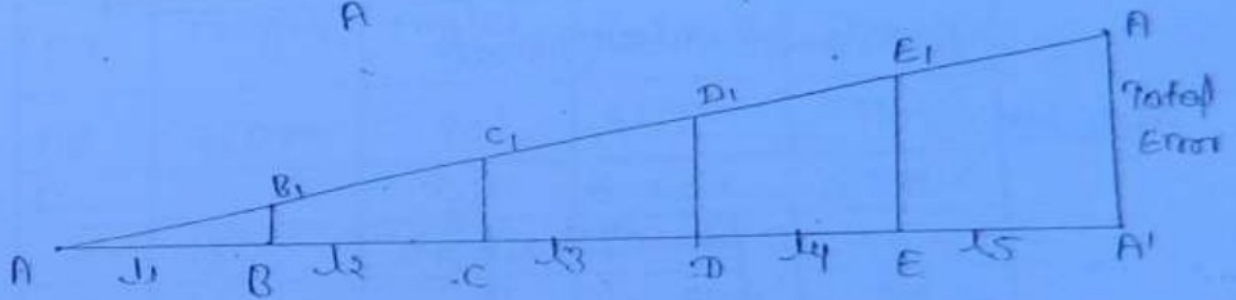
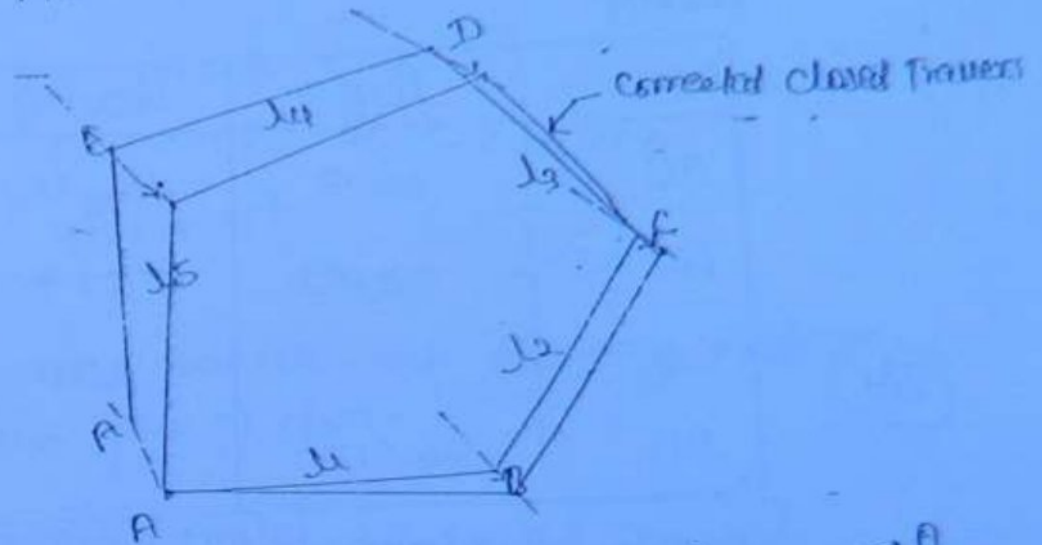
then correction in latitude of a part line

$$C_L = \Sigma L \times \frac{l_i}{L_T}$$

$$\text{--- } C_D = \Sigma D \times \frac{D_i}{D_T}$$

(2) Graphical method: →

(S3)



all this correction is made and the mark point is same direction.

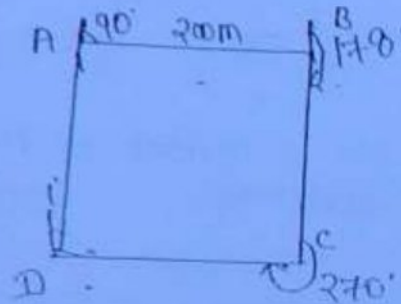
Ques: \rightarrow A closed traverse has the following length and bearing

Line	Length	Bearing
AB	200 m	Roughly East
BC	98 m	178°
CD	—	270°
DA	84.6 m	?

(34)

find out missing data

Solution: \rightarrow



Bearing	Latitude	Departure
Roughly East	$200 \cos 0$ $= -97.94$	$200 \sin 0$ $= 3.42$
178°	$x \cos 270 = 0$	$x \sin 270 = -x$
270°		
84.6	86.39	$= 1.500$
	$\Sigma L = 0$	$\Sigma D = 0$

From $\Sigma L = 0$

$$200 \cos 0 = 11.55$$

$$\cos 0 = 0.05775 \Rightarrow 0 = 86^\circ 41' 22'' \text{ Am}$$

$$\Sigma D = 0$$

$$200 \sin \theta + 3.42 + 1.508 - x = 0$$

$$x = 200 \sin 86^\circ 41' 22'' + 4.928$$

$$x = 204.60 \text{ m}$$

Ans

(5)

Problem: \rightarrow A closed traverse has following readings. Find out the missing data.

Line	Length	Angles w/c	Latitude	Departure
AB	250 m	85°	21.79	249.05
BC	- x	40°	0.766x	0.643x
CD	150	320°	114.907	-96.418
DE	220	295°	92.976	-179.39
EF	140	0° -	$140 \cos \theta$	$140 \sin \theta$
FA	200	160°	-187.94	68.404

Solution: \rightarrow

$$\Sigma L = 0$$

$$\Rightarrow 21.79 + 0.766x + 114.907 + 92.976 - 187.94 = 0 \quad \text{--- (1)}$$

$$\Sigma D = 0$$

$$249.05 - 0.643x - 96.418 - 179.39 + 68.404 = 0 \quad \text{--- (2)}$$

from eq. (1)

$$\Rightarrow 140 \cos \theta = -0.766x - 41.733 \quad \text{--- (3)}$$

from eq. (2)

$$\Rightarrow 140 \sin \theta = -0.643x - 21.646 \quad \text{--- (4)}$$

$$\Rightarrow 140^2 (\cos^2 \theta + \sin^2 \theta) = (0.768x + 41.733)^2 + (0.6432x + 21.646)^2$$

$$\Rightarrow 19600 = x^2 + 91.77x + 2210.192 = 0$$

$$\Rightarrow x^2 + 91.77x - 17389.8 = 0$$

$$\boxed{x = 93.74} \text{ m}$$

Ans

(56)

From eq. (3)

$$\cos \theta = -\frac{173.54}{140} = -0.81098$$

From eq. (4)

$$\sin \theta = -\frac{81.92}{140} = -0.58515$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = 0.7215$$

$$\theta = 35^\circ 45' 52''$$

Bearing of Line Line is in 3rd Q)

$$= 180 + \theta$$

$$= 180 + 35^\circ 48' 41.52''$$

$$\boxed{= 215^\circ 48' 41.52''}$$

Ans

