### Pulse width modulated inverters

The input dc voltage is of constant magnitude . The diode rectifier is used to rectify the line voltage. The inverter control the magnitude and frequency of the ac output voltage.

This is achieved by PWM technique of inverter switches and this is called PWM inverters.

The sinusoidal PWM technique is one of the PWM technique to shape the output voltage to as close as sinusoidal output.

## Basic concepts of switch mode inverter







During interval 1  $v_0$  and  $i_0$  both are positive

During interval 3  $v_0$  and  $i_0$  both are negative

Therefore during 1 and 3 the instantaneous power flow is from dc side to corresponding to inverter mode of operation.

In contrast during interval 2 and 4  $v_0$  and  $i_0$  are of opposite sign i.e. power flows from ac side to dc side corresponding to rectifier mode of operation.

## Pulse width modulated switching scheme

We require the inverter output to be sinusoidal with magnitude and frequency controllable.

In order to produce sinusoidal output voltage at desired frequency a sinusoidal control signal at desired frequency is compared with a triangular waveform as show.

The frequency of the triangular waveform established the inverter switching frequency.

The triangular waveform is called carrier waveform. The triangular waveform establishes switching frequency  $f_s$ , which establishes with which the inverter switches are applied.

The control signal has frequency  $f_s$  and is used to modulate the switch duty ratio.

 $f_1\;$  is the desired fundamental frequency of the output voltage.

## The amplitude modulation ratio $m_a$ is defined as

 $m_a = \frac{V_{control}}{V_{tri}}$ 

 $V_{control}$  is the peak amplitude of control signal.

 $V_{tri}$  peak amplitude of triangular signal.

## The frequency modulation ratio $m_f$



![](_page_3_Figure_0.jpeg)

When  $V_{control} > V_{tri}$   $T_A^+$  is ON  $V_{AO} = \frac{1}{2}V_d$ 

 $V_{control} < V_{tri}$   $T_A^-$  is ON  $V_{AO} = \frac{1}{2}V_d$ 

So the following inferences can be drawn

The peak amplitude of fundamental frequency is  $m_a times \frac{1}{2}V_d$ 

$$V_{AO} = m_{a} \frac{v_{d}}{\frac{2}{2}}$$

$$V_{AO} = \frac{V_{control}}{\hat{V}_{tri}} * \frac{v_{d}}{2} \qquad V_{control} \le \hat{V}_{tri}$$

# The foregoing arguments shown why V<sub>control</sub> is chosen to be sinusoidal to provide sinusoidal output voltage with fewer harmonics

Let the  $V_{control}$  vary sinusoidal with frequency  $f_1$ , which is the desired frequency of the inverter output voltage.

Let  $V_{control} = \widehat{V}_{control} sin \omega_1 t$ 

 $\widehat{V}_{control} \leq \widehat{V}_{tri}$ 

![](_page_4_Figure_0.jpeg)

$$\frac{\hat{v}_{tri}}{t_1} = \frac{\hat{V}_{tri}}{T_s/4}$$

At t= $t_1$ ,  $v_{tri}$ = $v_{control}$ 

So  $\frac{v_{control}}{t_1} = \frac{\hat{V}_{tri}}{T_s/4}$  $t_1 = \frac{\hat{v}_{control}}{\hat{V}_{tri}} * \frac{T_s}{4}$  $T_{on} = 2t_1 + \frac{T_s}{2}$  $D_1 = \frac{T_{on}}{T_s} = \frac{2t_1 + \frac{T_s}{2}}{2}$  $= \frac{1}{2} + \frac{2t_1}{T_s}$  $D_1 = \frac{1}{2} + \frac{2t_1}{2} (\frac{\hat{v}_{control}}{\hat{V}_{tri}})$ 

#### Three phase inverter

When three single-phase inverters are connected in parallel a three phase inverter is formed.

The gating signal has to be displaced by  $120^0$  with respect to each other so as achieve three phase balanced voltages.

A 3-phase output can be achieved from a configuration of six transistors and six diodes.

Two type of control signal can be applied to transistors, they are such as  $180^{0}$  or  $120^{0}$  conduction.

## 180-degree conduction

![](_page_5_Figure_2.jpeg)

When  $Q_1$  is switched on, terminal a is connected to the positive terminal of dc input voltage.

When  $Q_4$  is switched on terminal a is brought to negative terminal of the dc source.

There are 6 modes of operation is a cycle and the duration of each mode is  $60^{\circ}$ .

The conduction sequence of transistors is 123,234,345,456,561,612. The gating signals are shifted from each other by  $60^0$  to get 3- $\varphi$  balanced voltages.

## Switching states for the three phase voltage inverters